Converting Quadratic Equations between Standard and Vertex Form

Standard Form: $y = ax^2 + bx + c$ Vertex Form: $y = a(x - h)^2 + k$

Convert from Standard Form to Vertex Form:

$$y = ax^2 + bx = c$$
 \Longrightarrow $y = a(x - h)^2 + k$

know a, b, c

want a, h, k

$$x = \frac{-b}{2a} = h$$

Solve for y = k

Substitute the values and rewrite.

Example 1:

 $y = 8x^2 - 16x + 27$

 $h = x = \frac{-b}{2a} = \frac{-(-16)}{2(8)} = \frac{16}{16} = 1$

 $k = y = 8(1)^2 - 16(1) + 27 = 8 - 16 + 27 = 19$

 $y = 8(x-1)^2 + 19$

We know a, b, c and want a, h, k

a is the coefficient of the x2 term

use the formula to find the value of h

substitute the value found for h into the original equation and solve for k

Example 2:

$$y = 5x^2 - 40x + 67$$

$$a = 5$$

$$h = x = \frac{-b}{2a} = \frac{-(-40)}{2(5)} = \frac{40}{10} = 4$$

$$k = y = 5(4)^2 - 40(4) + 67 = 80 - 160 + 67 = -13$$

$$y = 5(x-4)^2-13$$

We know a, b, c and want a, h, k

a is the coefficient of the x^2 term

use the formula to find the value of h

substitute the value found for h into the original equation and solve for k

Practice: Convert the following quadratics from standard to vertex form.

1.
$$y = 5x^2 - 10x + 37$$

2.
$$y = 7x^2 + 28x + 19$$

3.
$$y = -2x^2 - 24x - 75$$



Convert from Vertex Form to Standard Form:

$$y = a(x - h)^2 + k$$
 \Longrightarrow $y = ax^2 + bx = c$

Example 1:

Example 2:

Practice: Convert the following quadratics from vertex to standard form.

1.
$$y = (x-2)^2 + 6$$

2.
$$y = 3(x-3)^2 - 12$$
 3. $y = -2(x+1)^2 + 3$

3.
$$v = -2(x+1)^2 + 3$$